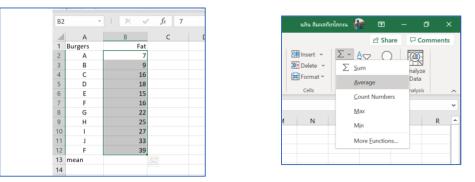


Variance (S<sup>2</sup>) = 
$$\frac{\sum (x_i - \overline{x})^2}{n-1}$$
 S =  $\sqrt{S^2}$  =  $\sqrt{\frac{\sum (x_i - \overline{x})^2}{n-1}}$   
Question: The following data represent the total fat for burgers items from a sample of fast-food chains. Find the variance, and standard deviation.  
7, 9, 16, 18, 15, 16, 22, 25 27, 33, 39

## **Sample Variance (S<sup>2</sup>)** Method 1:

Step 1 Enter all data in Excel software program

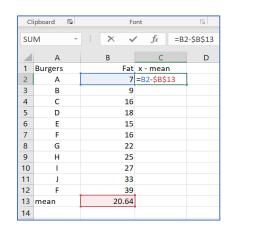
Step 2: Find the mean by using the AVERAGE function: =AVERAGE(B2:B12)

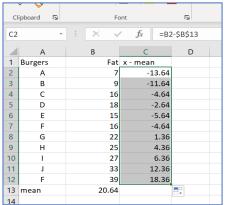


The average (mean) goes to any empty cell, say B13.

## Step 3: Subtract the mean (average) from each number in the sample:

- move cursor to column C2
- Type: =**B2-**\$**B**\$13 (mean value is in col **B**13, we will lock as a constant value)
- Click Enter. (You shall see the value of x-mean = -13.64 in column C2)
- move cursor to the corner of column C2 and drag until col C12





The differences go to column C, beginning in C2.

Step 4: Square each difference and put the results to column D, beginning in D2:

- Move cursor to column **D2**
- Type: =C2^2
- Click Enter. (You shall see the value of  $(x-mean)^2 = 185.9504$  in column D2)
- move cursor to the corner of column D2 and drag until col D12

				. <u>.</u> .		C	lipboard 🛛 🖓	Fc	ont	Ali Ali	gnment
D2	-		$f_x = C_x$	2^2		D	13	• : × •	f_x		
1	Α	В	С	D	E		A	В	с	D	E
1	Burgers	Fat	x - mean	(x-mean)^2		1	Burgers		x - mean	(x-mean)^2	
2	A	7	-13.64	185.9504		2	A	7	-13.64		
3	В	9	-11.64			3	B	9			
4	С	16	-4.64			4	C	16	-4.64		
5	D	18	-2.64			5	D	18	-2.64	6.9504	
6	E	15	-5.64			6	E	15	-5.64	31.7686	
7	F	16	-4.64			7	F	16	-4.64	21.4959	
8	G	22	1.36			8	G	22	1.36	1.8595	
9	н	25	4.36			9	н	25	4.36	19.0413	
0	1	27	6.36			10	- I	27	6.36	40.4959	
1	J	33	12.36			11	J	33	12.36	152.8595	
2	F	39	18.36			12	F	39	18.36	337.2231	
	mean	20.64				13	mean	20.64			
4		20101				14					
						15					

- **Step 5:** Add up the squared differences and divide the result by (n 1) or the number of items in the sample minus 1:
  - Move cursor to column **D15**
  - Type: =SUM(D2:D12)/(COUNT(B2:B12) 1)
  - or =SUM(D2:D12)/(11-1)
  - Click Enter. (You shall see the value of variance 95.5455 in column D15)

Cl	ipboard	12		Font	r <u>s</u>	Alignment
B2		*	$\geq$	< ✓ f <sub>x</sub>	=SUM(D2:D12)/(COUN	T(B2:B12)-1)
	А	В		с	D	E
1	Burgers		Fat	x-mean		
2	Α	Ī	7	-13.64	185.95	
3	В		9	-11.64	135.40	
4	С		16	-4.64	21.50	
5	D		18	-2.64	6.95	
6	E		15	-5.64	31.77	
7	F		16	-4.64	21.50	
8	G		22	1.36	1.86	
9	н		25	4.36	19.04	
10	1		27	6.36	40.50	
11	J		33	12.36	152.86	
12	F		39	18.36	337.22	
13	mean	20.	64			
14				SUM	954.55	
15				VAR	=SUM(D2:D12)/(COUN	(B2:B12)-1)
16						
17						

Cli	pboard IS	2	Font	L)	Alignment
C1	7	• E 🗦	< √ fx		
	А	В	С	D	E
1	Burgers	Fat	x-mean		
2	Α	7	-13.64	185.95	
3	В	9	-11.64	135.40	
4	С	16	-4.64	21.50	
5	D	18	-2.64	6.95	
6	E	15	-5.64	31.77	
7	F	16	-4.64	21.50	
8	G	22	1.36	1.86	
9	н	25	4.36	19.04	
10	1	27	6.36	40.50	
11	J	33	12.36	152.86	
12	F	39	18.36	337.22	
13	mean	20.64			
14			SUM	954.55	
15			Sample Var	95.45454545	
16					
17					
18					
10					

C	ipboard I	2	Font	5	Alignment
B2		* : 🗙	✓ fx =\	/AR.S(B2:B12)	
	А	В	С	D	
1	Burgers	Fat	x-mean	(x-mean)^2	
2	Α	7	-13.64	185.95	<i>.</i>
3	В	9	-11.64	135.40	)
4	С	16	-4.64	21.50	)
5	D	18	-2.64	6.95	i
6	E	15	-5.64	31.77	/
7	F	16	-4.64	21.50	)
8	G	22	1.36	1.86	ذ
9	н	25	4.36	19.04	4
10	- I	27	6.36	40.50	)
11	J	33	12.36	152.86	ذ
12	F	39	18.36	337.22	2
13	mean	20.64			
14			SUM	954.55	<b>i</b>
15			Sample Var	95.45454545	<b>i</b>
16					
17		Method 2	Sample Var	=VAR.S(B2:B12)	
18					

Method 2:	Move cursor to D17 or	r any empty space and Type:	=VAR.S(B2:B12)
-----------	-----------------------	-----------------------------	----------------

Cl	ipboard f	2	Font	ا <u>د</u> ا		Alignme
B1	7	• = ×	$\checkmark f_x$	Method 2		
	А	В	с		D	
1	Burgers	Fat	x-mean	(x-	mean)^2	
2	Α	7	-13.0	54	185.95	
3	В	9	-11.0	54	135.40	
4	С	16	-4.0	54	21.50	
5	D	18	-2.0	54	6.95	
6	E	15	-5.6	54	31.77	
7	F	16	-4.0	54	21.50	
8	G	22	1.3	36	1.86	
9	н	25	4.3	36	19.04	
10	1	27	6.3	36	40.50	
11	J	33	12.3	36	152.86	
12	F	39	18.3	36	337.22	
13	mean	20.64				
14			SUM		954.55	
15			Sample Var		95.45454545	
16						
17		Method 2	Sample Var		95.45454545	
18						
19						

b) Find the value of sample standard deviation:

Find the value of **sample standard deviation**:

- Move cursor to column **D18**
- Type: **=SQRT(D17**)
- Click Enter.

You shall see the value of sample standard deviation 9.770084209 in column D18

Cli	pboard I	2	Font	E2	Alignment
D1	8	• : ×	$\checkmark f_x =$	SQRT(D17)	
	А	В	с	D	E
1	Burgers	Fat	x-mean	(x-mean)^2	
2	Α	7	-13.64	185.95	5
3	В	9	-11.64	135.40	)
4	С	16	-4.64	21.50	)
5	D	18			
6	E	15			
7	F	16			
8	G	22			
9	н	25			
10	- I	27			
11	J	33			
12	F	39		337.22	2
13	mean	20.64			
14			SUM	954.55	
15			Sample Var	95.45454545	5
16					
17		Method 2	Sample Var	95.45454545	
18			Standard Dev	9.770084209	
19					
20					

Sample Variance of fast-food chains = 95.4545

Sample standard deviation = 9.77